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Work in collaboration with:

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Black hole radiation spectrum in Loop Quantum Gravity



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CONTENTS



Introduction

CONTENTS

Introduction

Black holes in Loop Quantum Gravity

Black hole entropy

CONTENTS

Introduction

Black holes in Loop Quantum Gravity

Black hole entropy

Computational counting

CONTENTS

Introduction

Black holes in Loop Quantum Gravity

Black hole entropy

Computational counting

Discretization

CONTENTS

Introduction

Black holes in Loop Quantum Gravity

Black hole entropy

Computational counting

Discretization

Spectroscopy

CONTENTS

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Spectroscopy

Conclusions

Future lines

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Here: Some different new results.

BLACK HOLES IN LQG

[A.Ashtekar, J.Baez, A.Corichi, K.Krasnov]

Inner boundary introduced in the spacetime manifold before quantization procedure (*effective treatment*)

Isolated horizon boundary conditions

Hilbert space splitting: $H_v \otimes H_s$

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Surface states: U(1) Chern-Simons theory over a punctured sphere

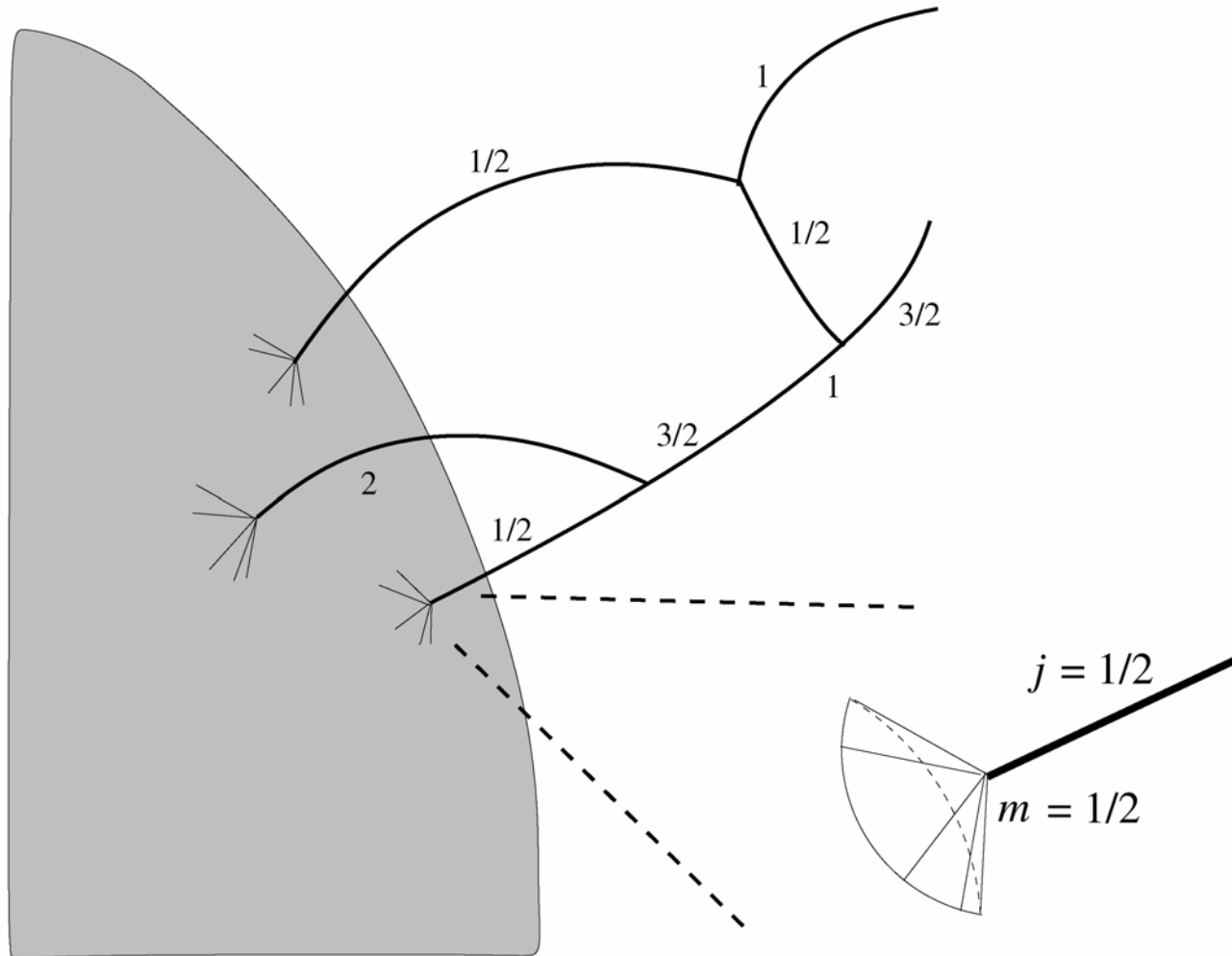
Spin network pierces the horizon at punctures

Punctures carry some quantum labels satisfying

$$\sum_i m_i = 0 \quad (\text{projection constraint})$$

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Result:
$$S = \frac{1}{4} A - \frac{1}{2} \ln A$$
 up to γ .

COMPUTATIONAL COUNTING

A. Corichi, E. Fernandez-Borja, J.D. [Class. Quantum Grav. **24**, 243 (2007)]

In order to make an **exact counting** we use an explicit enumeration algorithm

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But **linear dependence** and **logarithmic correction** are obtained \Rightarrow some confidence

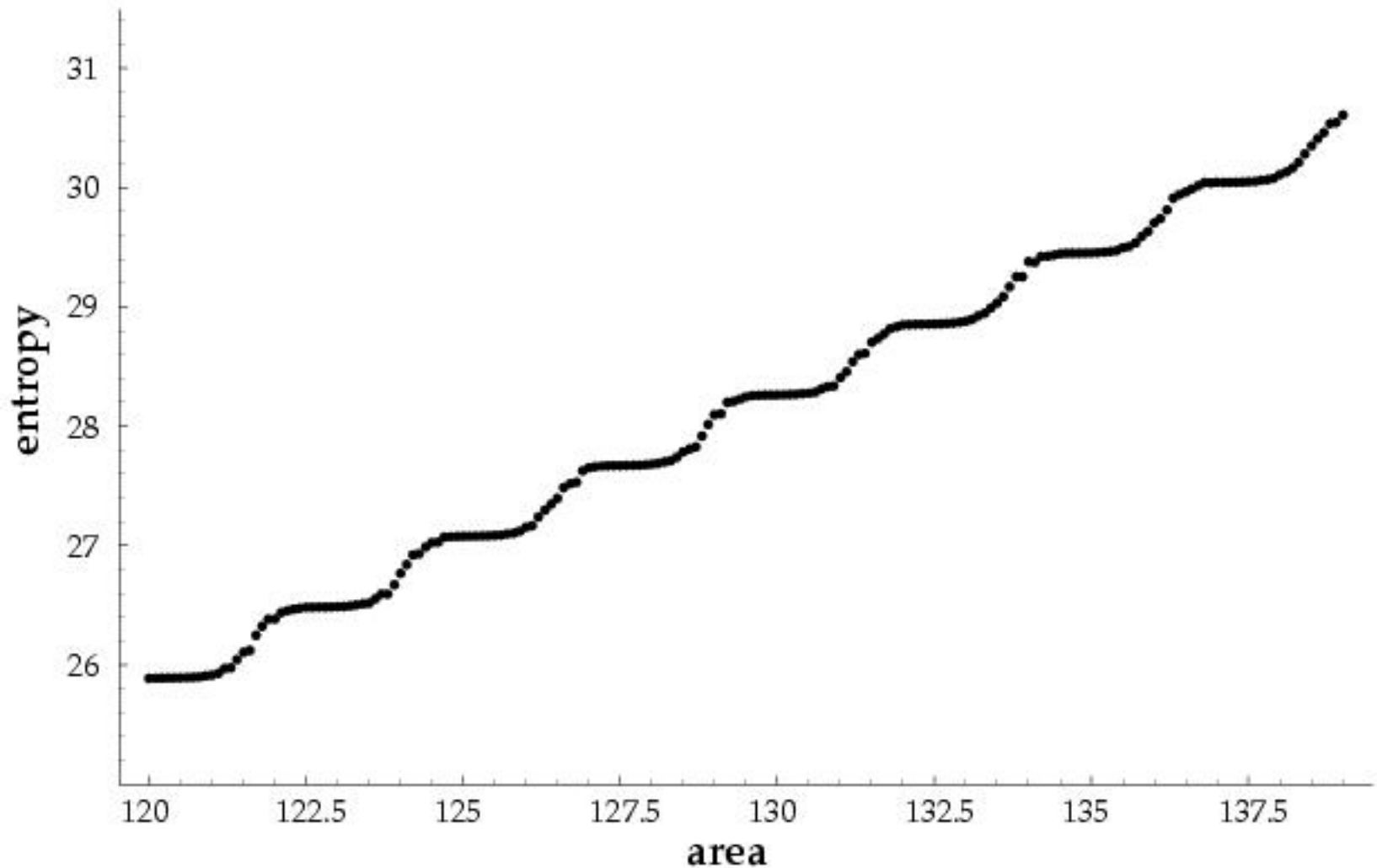
DISCRETIZATION

A. Corichi, E. Fernandez-Borja, J.D. [Phys. Rev. Lett. **98**, 181301 (2007)]

Surprising new behaviour of entropy as an area function: **stair-like structure**

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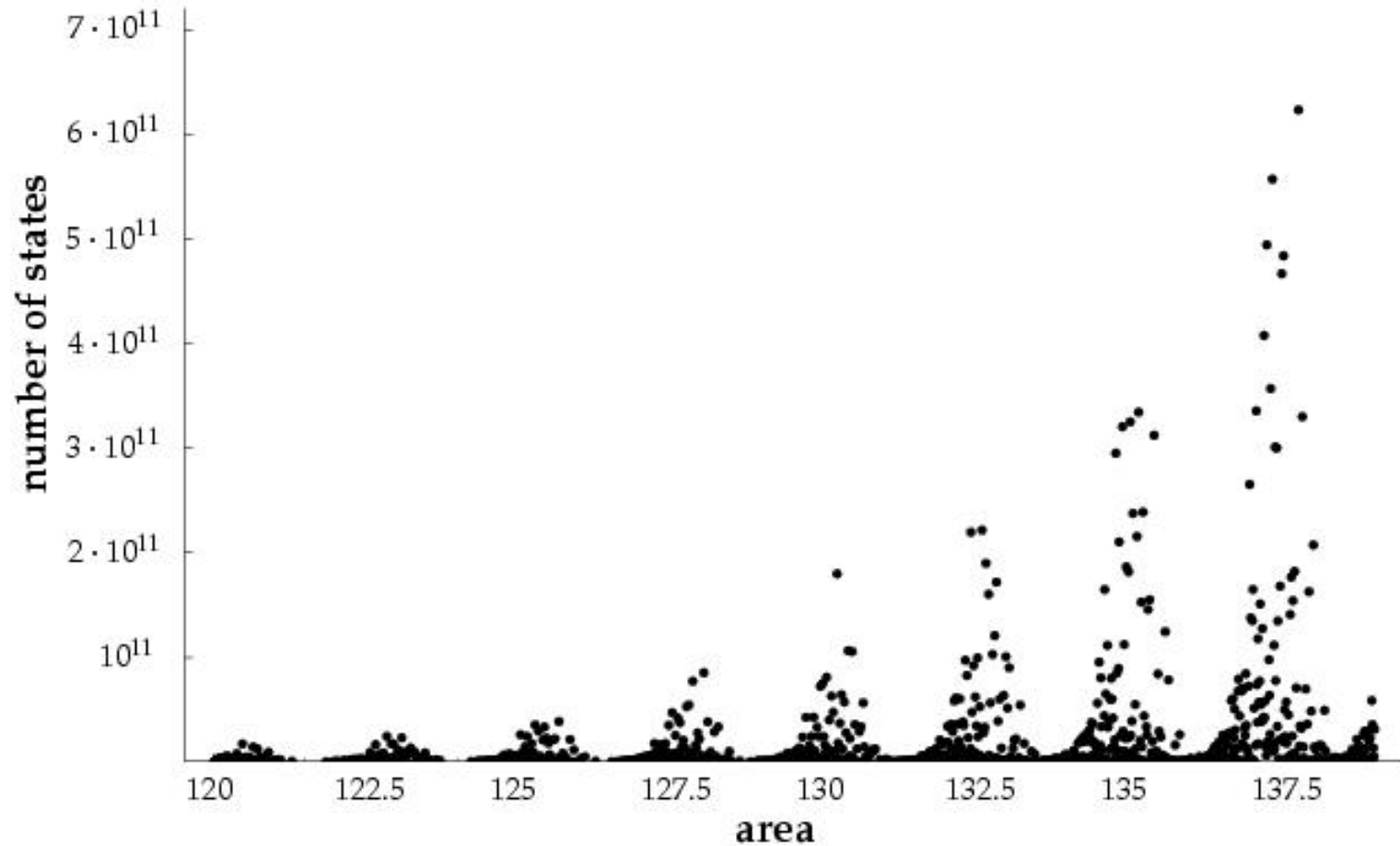
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Where this behaviour comes from?

DISCRETIZATION

Structure of the horizon area eigenstate degeneracy
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Structure with “bands” or peaks of degeneracy

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With this: - Explanation for the staircase

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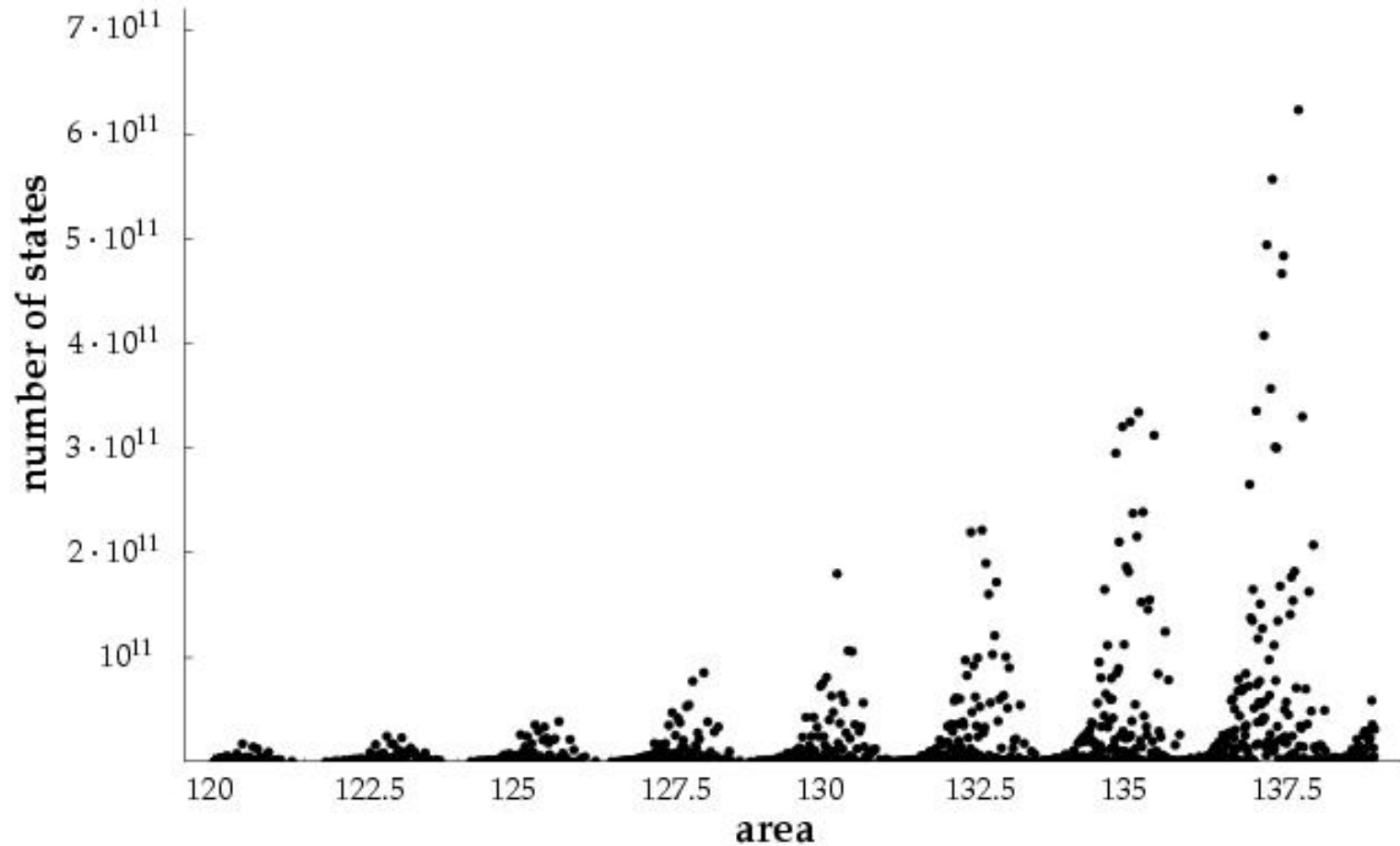
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With this: - Explanation for the staircase

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Consider **all possible transitions** regardless of the concrete quantum configuration (unknown dynamics)

DISCRETIZATION



SPECTROSCOPY ("toy model")

E.Fernandez-Borja, J.D. [arXiv: 0706.1979 [gr-qc]]

First approximation: consider only states at the peaks

Equidistant area spectrum with a gap $\Delta A = \chi \gamma \ell_P^2$

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Analogous to Bekenstein-Mukhanov picture

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- The spectrum is **not discrete**
- Statistically preferred frequencies
- Equidistant “**brighter**” lines sticking out from a **continuous background spectrum**
- The bands are not narrow \Rightarrow **Broadening** of the lines

CONCLUSIONS

We make an spectroscopical analysis at the **kinematical level** (we don't know dynamics)

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Observable **qualitative effects** in the spectrum

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ω_0 proportional to $\gamma \Rightarrow$ hypothetical observational determination (GRB's ???)

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